
Automated Generation of Decision Table and Boundary Values from VDM++ Specification

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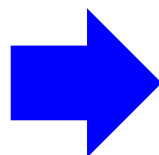
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1. background
2. VDTTable
3. BWDM
4. Conclusion

VDM + Decision Table = VDTTable

VDM++
Specification



CLASS
VDTTable

- summation
- NatSeqSum
- bin2dec
- revBin2dec
- rev
- Add01
- length

```

001 class Sample
002
003 functions
004 summation( n:nat, a:seq of nat) s:nat
005 pre (n = len a) and (n >= 1)
006 post s = NatSeqSum( a );
007
008 NatSeqSum: (seq of nat) -> nat
009 NatSeqSum( s ) ==
010 cases s :
011 [] -> 0,
012 others -> hd s + NatSeqSum( tl s )
013 end;
014
015 bin2dec : seq of nat -> nat
016 bin2dec(s) ==
017 revBin2dec( rev(s) );
018
019 revBin2dec : seq of nat -> nat
020 revBin2dec( s ) ==
021 cases s :
022 [] -> 0,
023 [0] -> 0,
024 [1] -> 1,
025 others -> hd s + 2*revBin2dec( tl s )
026 end;
027
                    
```

{P}
A
{Q}

Rule	#1	#2
Pre Condition		
((n = (len a) and (n >= 1))	Y	N
Action		
summation	X	-

Decision
Table

Rule	#1	#2
Pre Condition		
((n = (len a) and (n >= 1))	Y	N
Action		
summation	X	-

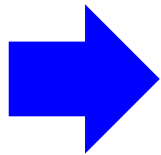
class name : Sample					
function name : SampleFunction					
		#1	#2	#3	#4
Condition	a < 5	T	T	F	F
Condition	12 <= a	T	F	T	F
Action	"a < 5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5 <= a < 12"	F	F	F	T

1. **Condition part** – Describe the conditional expressions in software and the possible combinations of these Boolean values
2. **Action part** – Describe the operation in the software and the action on the truth value of the condition part
3. **Rule part** – Describe Behavior of software between condition part and action part

Boundary Value + Vienna Development Method = BWDM

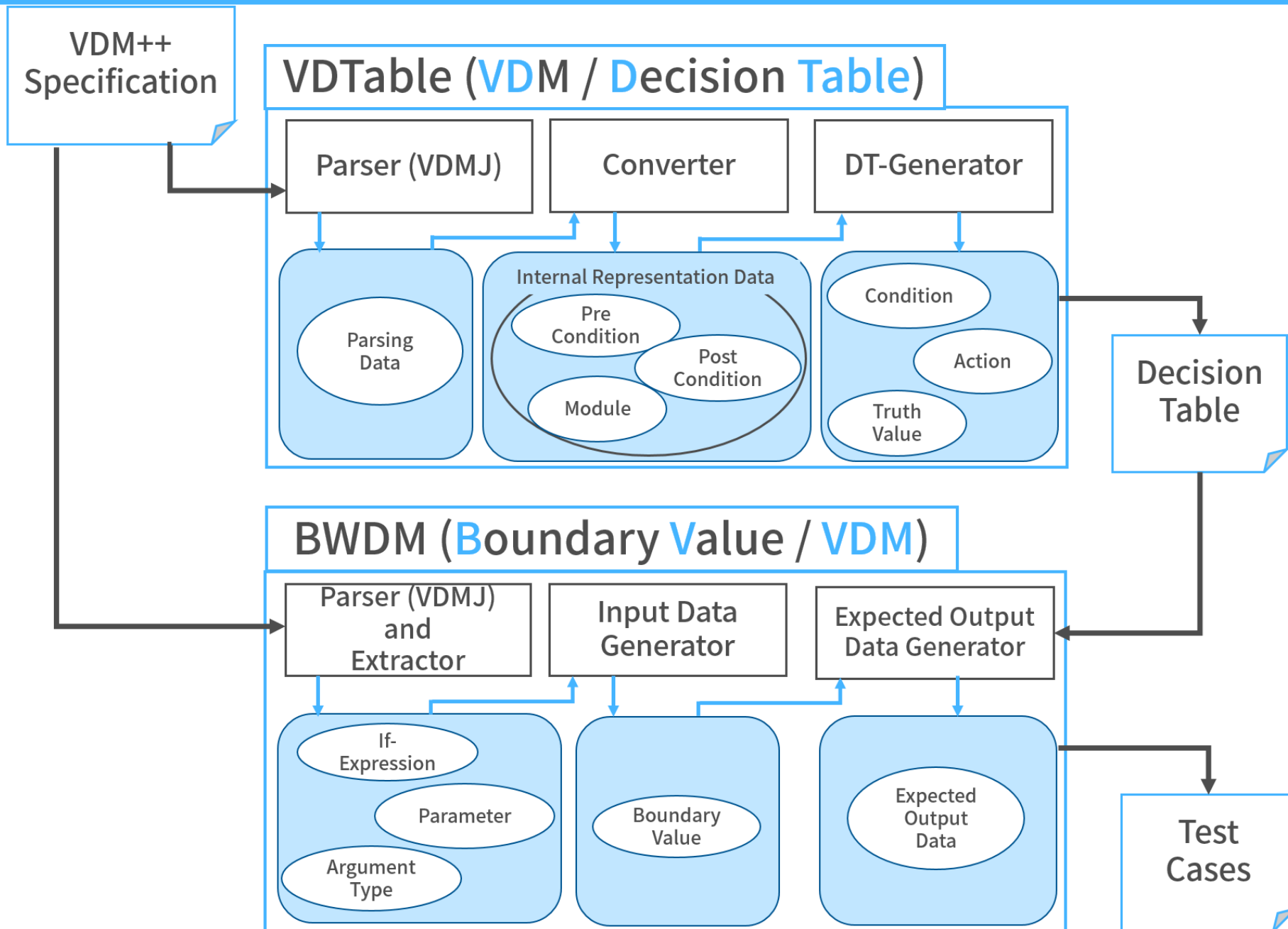
VDM++
Specification

Decision
Table



No.	Input	Output	Action
No.5	natMin-1	0	Undefined Action
No.6	natMin-1	-1	Undefined Action
No.7	natMin	intMin-1	Undefined Action
No.8	natMin	intMin	arg1:even arg2:negative
No.9	natMin	intMax	arg1:even arg2:positive
No.10	natMin	intMax+1	Undefined Action
No.11			arg1:even arg2:positive
No.12			arg1:even arg2:negative
No.13			Undefined Action
No.14			arg1:odd arg2:negative
No.15			arg1:odd arg2:positive
No.16			Undefined Action
No.17			arg1:odd arg2:positive
No.18			arg1:odd arg2:negative
No.19			Undefined Action
No.20	natMax+1	intMin	Undefined Action
No.21	natMax+1	intMax	Undefined Action
No.22	natMax+1	intMax+1	Undefined Action
No.23	natMax+1	0	Undefined Action
No.24	natMax+1	-1	Undefined Action
No.25	2	intMin-1	Undefined Action
No.26	2	intMin	arg1:even arg2:negative
No.27	2	intMax	arg1:even arg2:positive
No.28	2	intMax+1	Undefined Action
No.29	2	0	arg1:even arg2:positive
No.30	2	-1	arg1:even arg2:negative
No.31	1	intMin-1	Undefined Action
No.32	1	intMin	arg1:odd arg2:negative
No.33	1	intMax	arg1:odd arg2:positive

Test Cases



input

output

VDM++
Specification

VDTable (VDM / Decision Table)

Parser (VDMJ)

Converter

DT-Generator

Parsing
Data

Internal Representation Data

Pre
Condition

Post
Condition

Module

Condition

Action

Truth
Value

Decision
Table

D-Tree

VS-Screen

The screenshot shows the VTable application interface. On the left, a class hierarchy is displayed under the heading 'CLASS'. The 'summation' class is selected, showing its methods: NatSeqSum, bin2dec, revBin2dec, rev, Add01, and length. The main area is a code editor showing the implementation of these methods. The code is as follows:

```
001 class Sample
002
003 functions
004 summation( n:nat, a:seq of nat) s:nat
005 pre (n = len a) and (n >= 1)
006 post s = NatSeqSum( a );
007
008 NatSeqSum: (seq of nat) -> nat
009 NatSeqSum( s ) ==
010 cases s :
011 [] -> 0,
012 others -> hd s + NatSeqSum( tl s )
013 end;
014
015 bin2dec : seq of nat -> nat
016 bin2dec(s) ==
017 revBin2dec( rev(s) );
018
019 revBin2dec : seq of nat -> nat
020 revBin2dec( s ) ==
021 cases s :
022 [] -> 0,
023 [0] -> 0,
024 [1] -> 1,
025 others -> hd s + 2*revBin2dec( tl s )
026 end;
```

At the bottom, a decision table is shown. It has columns for Rule, #1, and #2. The table contains the following data:

Rule	#1	#2
Pre Condition		
((n = (len a) and (n >= 1))	Y	N
Action		
summation	X	-

DT-Panel

A: module tab

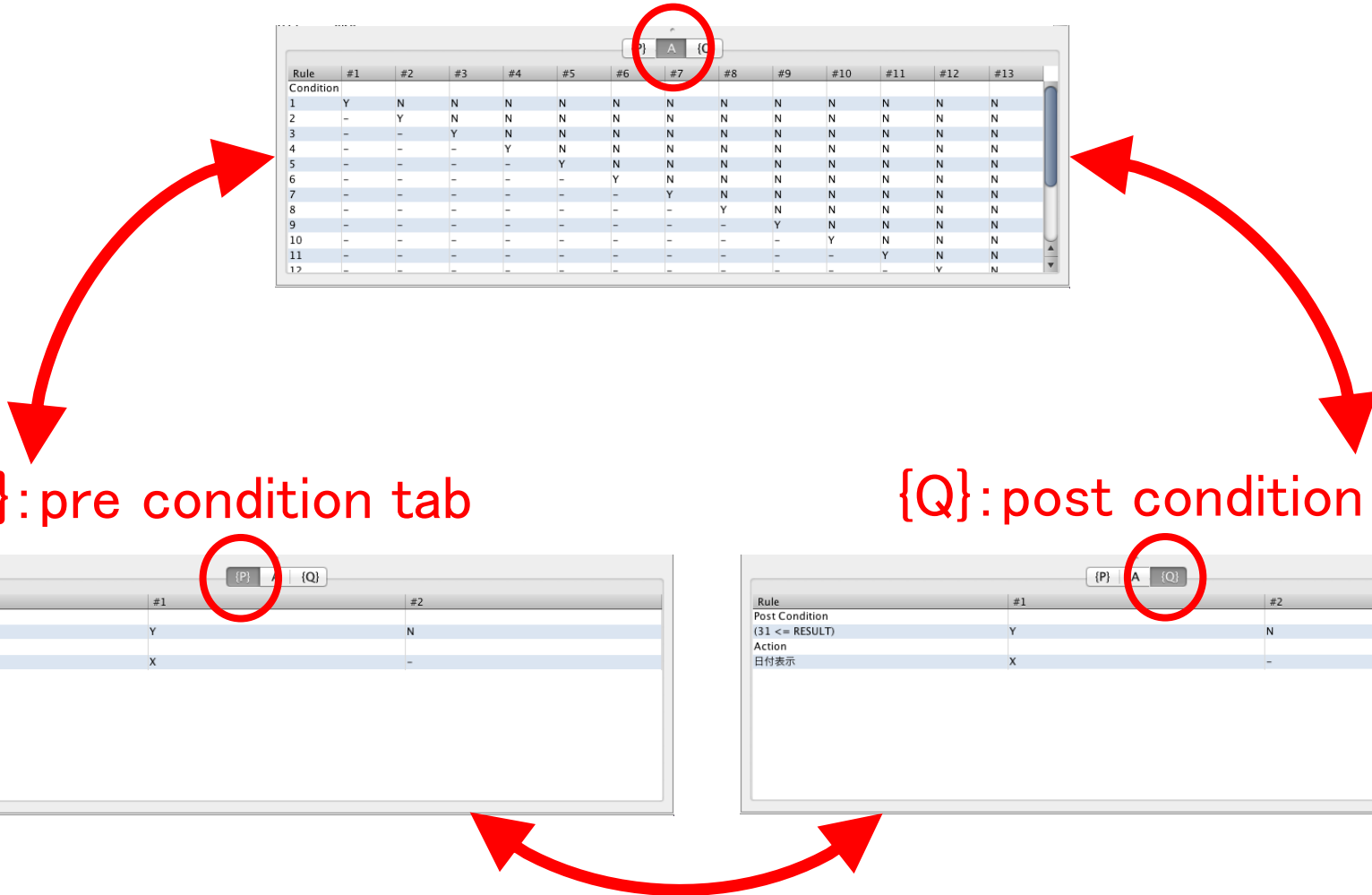
Rule	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
1	Y	N	N	N	N	N	N	N	N	N	N	N	N
2	-	Y	N	N	N	N	N	N	N	N	N	N	N
3	-	-	Y	N	N	N	N	N	N	N	N	N	N
4	-	-	-	Y	N	N	N	N	N	N	N	N	N
5	-	-	-	-	Y	N	N	N	N	N	N	N	N
6	-	-	-	-	-	Y	N	N	N	N	N	N	N
7	-	-	-	-	-	-	Y	N	N	N	N	N	N
8	-	-	-	-	-	-	-	Y	N	N	N	N	N
9	-	-	-	-	-	-	-	-	Y	N	N	N	N
10	-	-	-	-	-	-	-	-	-	Y	N	N	N
11	-	-	-	-	-	-	-	-	-	-	Y	N	N
12	-	-	-	-	-	-	-	-	-	-	-	Y	N

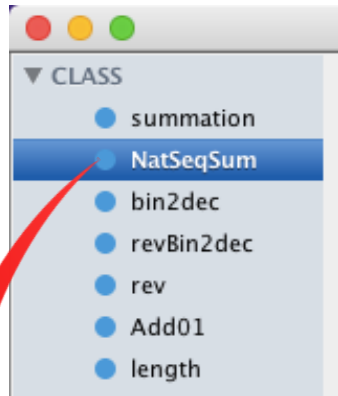
{P}: pre condition tab

Rule	#1	#2
Pre Condition (月 <= 12)	Y	N
Action		
日付表示	X	-

{Q}: post condition tab

Rule	#1	#2
Post Condition (31 <= RESULT)	Y	N
Action		
日付表示	X	-

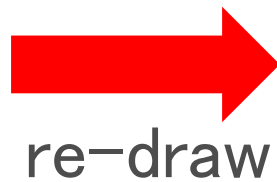
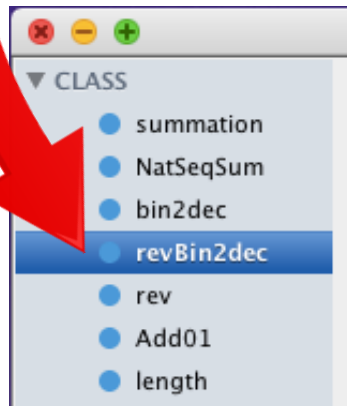




A screenshot of a decision table window. At the top, there are three buttons: {P}, A, and {Q}. The table has three columns: Rule, #1, and #2. The rows are as follows:

Rule	#1	#2
Condition		
[]	Y	N
Action		
0	X	-
((hd s) + NatSeqSum((tl s)))	-	X

click any definition



A screenshot of a decision table window. At the top, there are three buttons: {P}, A, and {Q}. The table has five columns: Rule, #1, #2, #3, and #4. The rows are as follows:

Rule	#1	#2	#3	#4
Condition				
[]	Y	N	N	N
[0]	-	Y	N	N
[1]	-	-	Y	N
Action				
0,	X	X	-	-
1	-	-	X	-
((hd s) + (2 * revBin2dec((tl s))))	-	-	-	X

```
class Day
functions
public dateDisp: nat1 * nat1 -> nat1
  dateDisp(year, month) ==
    cases month:
      1 -> 31,
      2 -> judgeLeapYear (year),
      3 -> 31,
      4 -> 30,
      5 -> 31,
      6 -> 30,
      7 -> 31,
      8 -> 31,
      9 -> 30,
      10 -> 31,
      11 -> 30,
      12 -> 31,
      others -> undefined
end;
```

...

Day specification

- ✓ Inputs are year and month.
- ✓ Return value is the date at the end of the month of the input.
year / month.
- ✓ If it was entered a month other than January to December, the return value is an undefined expression.
- ✓ condition : 12
 - 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12
- ✓ action : 4
 - 31 judgeLeapYear (year), 30, undefined

The screenshot shows the VTable application interface. On the left, a tree view shows the project structure with 'CLASS', 'dateDisp', and 'judgeLeapYear' folders. The main area displays source code for a class named 'Day'. The code includes methods for 'dateDisp' and 'judgeLeapYear', with various conditional branches based on month and year properties. Below the code, a decision table (DT-Panel) is generated, showing 13 rules and their corresponding actions.

```
001 class Day
002
003 functions
004
005 public dateDisp:nat1* nat1 -> nat1
006   dateDisp (year, month) ==
007     cases month:
008       1 -> 31,
009       2 -> judgeLeapYear (year),
010       3 -> 31,
011       4 -> 30,
012       5 -> 31,
013       6 -> 30,
014       7 -> 31,
015       8 -> 31,
016       9 -> 30,
017       10 -> 31,
018       11 -> 30,
019       12 -> 31,
020     others -> undefined
021   end;
022
023 public judgeLeapYear:nat1 -> nat1
024   judgeLeapYear (year) ==
025     if (year mod 4 = 0) then
026       if (year mod 100 = 0) then
027         if (year mod 400 = 0) then 29
028         else 28
029       else 29
030     else 28;
031
032 end Day
```

(P)	A	(Q)	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
Condition															
1			Y	N	N	N	N	N	N	N	N	N	N	N	N
2			-	Y	N	N	N	N	N	N	N	N	N	N	N
3			-	-	Y	N	N	N	N	N	N	N	N	N	N
4			-	-	-	Y	N	N	N	N	N	N	N	N	N
5			-	-	-	-	Y	N	N	N	N	N	N	N	N
6			-	-	-	-	-	Y	N	N	N	N	N	N	N
7			-	-	-	-	-	-	Y	N	N	N	N	N	N
8			-	-	-	-	-	-	-	Y	N	N	N	N	N
9			-	-	-	-	-	-	-	-	Y	N	N	N	N
10			-	-	-	-	-	-	-	-	-	Y	N	N	N
11			-	-	-	-	-	-	-	-	-	-	Y	N	N
12			-	-	-	-	-	-	-	-	-	-	-	Y	N
Action															
31	X		-	-	X	-	X	-	X	X	-	X	-	X	-
judgeLeapYea...	-		X	-	-	-	-	-	-	-	-	-	-	-	-
30	-		-	-	-	X	-	X	-	-	X	-	X	-	-
(undefined)	-		-	-	-	-	-	-	-	-	-	-	-	-	X

 generated decision table (DT-Panel)

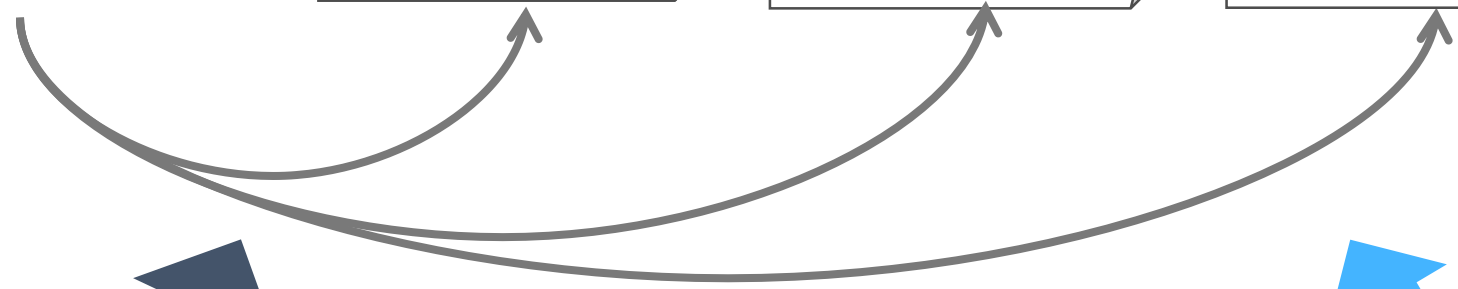
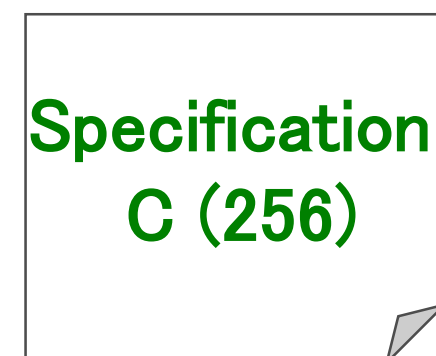
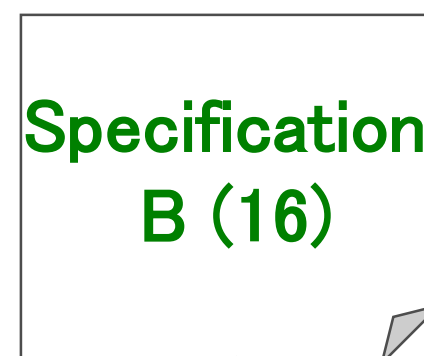
12 conditions and 4 actions (all conditions and actions) are extracted.

Rule	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
Condition													
1	Y	N	N	N	N	N	N	N	N	N	N	N	N
2	-	Y	N	N	N	N	N	N	N	N	N	N	N
3	-	-	Y	N	N	N	N	N	N	N	N	N	N
4	-	-	-	Y	N	N	N	N	N	N	N	N	N
5	-	-	-	-	Y	N	N	N	N	N	N	N	N
6	-	-	-	-	-	Y	N	N	N	N	N	N	N
7	-	-	-	-	-	-	Y	N	N	N	N	N	N
8	-	-	-	-	-	-	-	Y	N	N	N	N	N
9	-	-	-	-	-	-	-	-	Y	N	N	N	N
10	-	-	-	-	-	-	-	-	-	Y	N	N	N
11	-	-	-	-	-	-	-	-	-	-	Y	N	N
12	-	-	-	-	-	-	-	-	-	-	-	Y	N
Action													
31	X	-	X	-	X	-	X	X	-	X	-	X	-
judgeLeapYea..	-	X	-	-	-	-	-	-	-	-	-	-	-
30	-	-	-	X	-	X	-	-	X	-	X	-	-
(undefined)	-	-	-	-	-	-	-	-	-	-	-	-	X

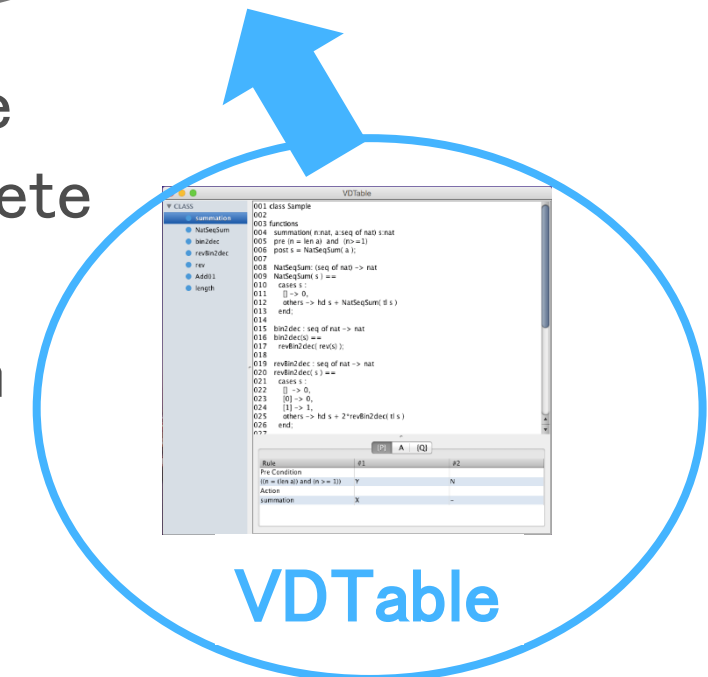
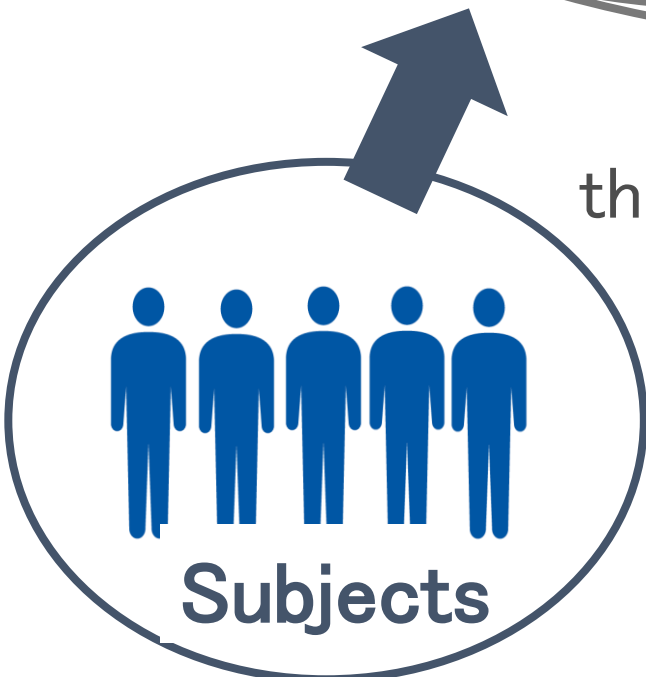
Truth values are properly generated.

We confirmed that the VTable operates correctly.

The number of combination of truth values is different



Measure and compare the time taken to complete the decision table for each specification



VTable

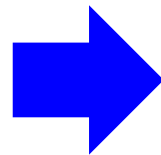
subject	VDM++ specification (The number of combination of truth values)		
	specification A (4)	specification B (16)	specification C (256)
A	252	405	1131
B	213	559	1292
C	169	499	1194
D	240	435	1859
E	134	557	1397
average	216	498	1629
VTable	0.012	0.016	0.02

- VTable reduced labor and time for manual work.
- VTable is useful for improving the work of designing a decision table using the VDM++ specification.

Boundary Value + Vienna Development Method = BWDM

VDM++
Specification

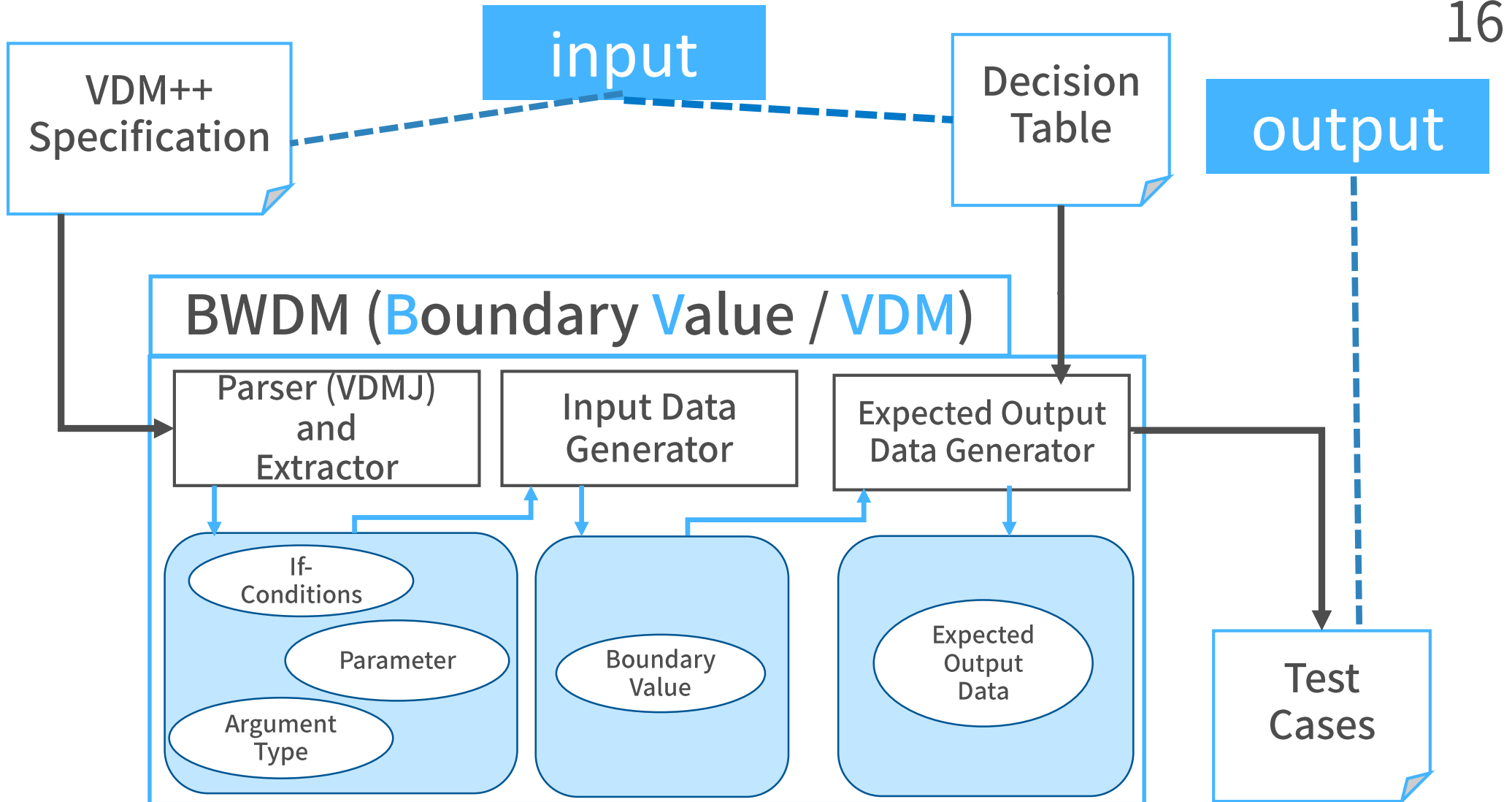
Decision
Table

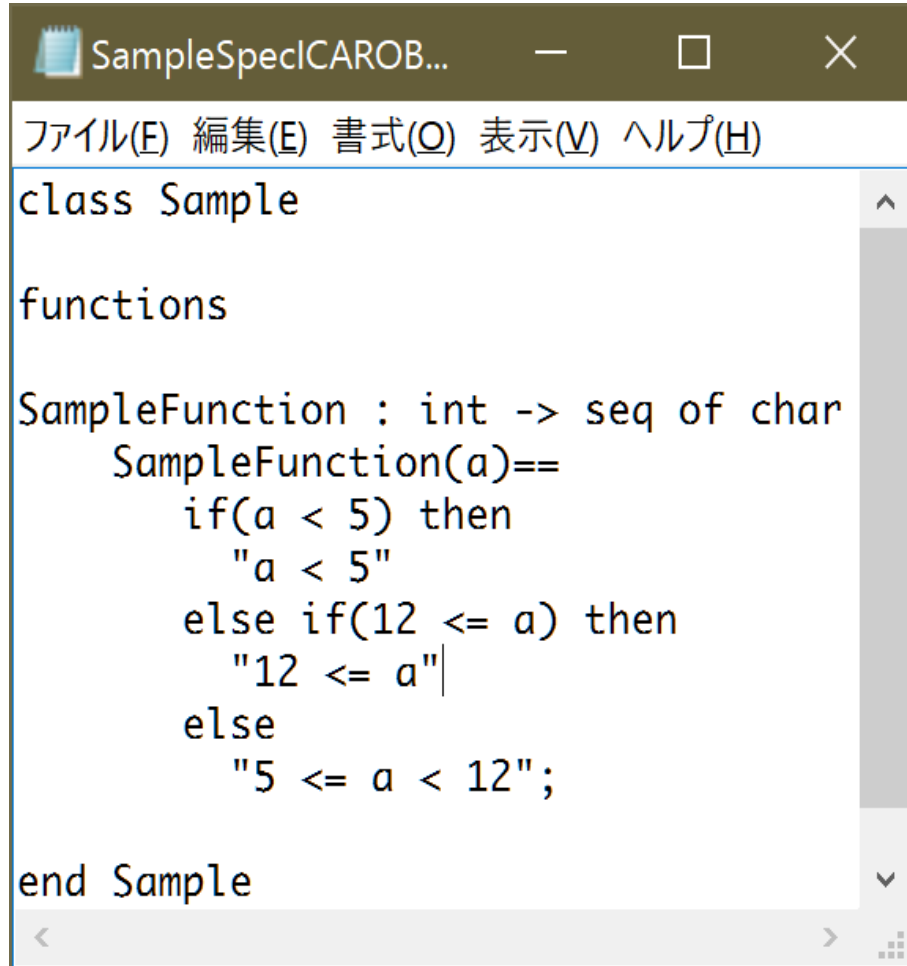


No.5	natMin-1	0	-->	Undefined Action
No.6	natMin-1	-1	-->	Undefined Action
No.7	natMin	intMin-1	-->	Undefined Action
No.8	natMin	intMin	-->	arg1:even arg2:negative
No.9	natMin	intMax	-->	arg1:even arg2:positive
No.10	natMin	intMax+1	-->	Undefined Action
No.11	natMin	0	-->	arg1:even arg2:positive
No.12				arg1:even arg2:negative
No.13				Undefined Action
No.14				arg1:odd arg2:negative
No.15				arg1:odd arg2:positive
No.16				Undefined Action
No.17				arg1:odd arg2:positive
No.18				arg1:odd arg2:negative
No.19				Undefined Action
No.20				Undefined Action
No.21				Undefined Action
No.22	natMax+1	intMax+1	-->	Undefined Action
No.23	natMax+1	0	-->	Undefined Action
No.24	natMax+1	-1	-->	Undefined Action
No.25	2	intMin-1	-->	Undefined Action
No.26	2	intMin	-->	arg1:even arg2:negative
No.27	2	intMax	-->	arg1:even arg2:positive
No.28	2	intMax+1	-->	Undefined Action
No.29	2	0	-->	arg1:even arg2:positive
No.30	2	-1	-->	arg1:even arg2:negative
No.31	1	intMin-1	-->	Undefined Action
No.32	1	intMin	-->	arg1:odd arg2:negative

Test Cases

BWDM outputs test cases that based on boundary value analysis.





```
SampleSpecCAROB...
ファイル(E) 編集(E) 書式(O) 表示(V) ヘルプ(H)
class Sample
functions
SampleFunction : int -> seq of char
  SampleFunction(a)==
    if(a < 5) then
      "a < 5"
    else if(12 <= a) then
      "12 <= a"
    else
      "5 <= a < 12";
end Sample
```

- a function definition in VDM++ specification
- an argument of int
- return value is Sequence of char
- two if-conditions

VDM++ specification

```
SampleSpecCAROB...
ファイル(E) 編集(E) 書式(O) 表示(V) ヘルプ(H)
class Sample
functions
SampleFunction : int -> seq of char
SampleFunction(a)==
  if(a < 5) then
    "a < 5"
  else if(12 <= a) then
    "12 <= a"
  else
    "5 <= a < 12"
end Sample
```

Type Boundary Value

if-condition

boundary value

Boundary Value Analysis

Expected Output Data of outside input values of type range

Test Case No.	Input Data	Expected Output Data
No.1	intMin-1	"Undefined Action"
No.2	intMin	"a < 5"
No.3	intMax	"12 <= a"
No.4	intMax+1	"Undefined Action"
No.5	4	"a < 5"
No.6	5	"5 < a <= 12"
No.7	11	"5 < a <= 12"
No.8	12	"12 <= a"

VDM++ Specification

test cases

Input Data

- Generated from function definition in VDM++ specification.
- Consists of 2 kind of boundary value; **type boundary value** that is generated from arguments type, and **if-conditions boundary value** that is generated from if conditions.

type boundary value

Ex.) When the argument of the function is an int



intMin, intMax, intMin-1, intMax+1

Minimum, maximum, and outside values of
Integer range

In testing phase, tester corrects it to actual numbers, such as intMin:-2147483648, according to the development environment (language, bit number, etc.), and performs test.

if-conditions boundary value

Ex.) When the if-condition is "a<4"



3, 4 (3:true, 4:false)

two integer values at the boundary of the inequality (three values when if-condition is modulo)

Expected Output Data

- Output when input data is input to program
- When receiving outside values of type range (*Min-1, *Max+1), the program overflows and the operation can not be predicted so the expected output data is assumed to be “Undefined Action”.

```
SampleSpecCAROB...
ファイル(E) 編集(E) 書式(O) 表示(V) ヘルプ(H)
class Sample
functions
SampleFunction : int -> seq of char
SampleFunction(a)==
  if(a < 5) then
    "a < 5"
  else if(12 <= a) then
    "12 <= a"
  else
    "5 <= a < 12"
end Sample
```

Type Boundary Value

if-condition

boundary value

Boundary Value Analysis

Expected Output Data of outside input values of type range

Test Case No.	Input Data	Expected Output Data
No.1	intMin-1	"Undefined Action"
No.2	intMin	"a < 5"
No.3	intMax	"12 <= a"
No.4	intMax+1	"Undefined Action"
No.5	4	"a < 5"
No.6	5	"5 < a <= 12"
No.7	11	"5 < a <= 12"
No.8	12	"12 <= a"

VDM++ Specification

test cases

Mixed inequality and modulo

```
class MixSpecification
```

```
  functions
```

```
  mix: nat * int -> seq of char
    mix( arg1 , arg2 ) ==
      if( arg1 mod 2 = 0 ) then
        if ( 0 <= arg2 ) then
          " arg1:even arg2:positive"
        else
          " arg1:even arg2:negative"
        else
          if( arg2 < 0 ) then
            " arg1:odd arg2:negative"
          else
            " arg1:odd arg2:positive";
```

```
end MixSpecification
```

- two arguments
- determine whether arg1 is an even number in the first remainder expression
- In two inequalities, it judges the sign of arg2

The number of arguments:2

argument type: argument1:nat argument2:int

No.	input data	-->	expected output data
No.1	natMin-1	intMin-1	--> Undefined Action
No.2	natMin-1	intMin	--> Undefined Action
No.3	natMin-1	intMax	--> Undefined Action
No.4	natMin-1	intMax+1	--> Undefined Action
No.5	natMin-1	0	--> Undefined Action
No.6	natMin-1	-1	--> Undefined Action
No.7	natMin	intMin-1	--> Undefined Action
No.8	natMin	intMin	--> arg1:even arg2:negative
No.9	natMin	intMax	--> arg1:even arg2:positive
No.10	natMin	intMax+1	--> Undefined Action
No.11	natMin	0	--> arg1:even arg2:positive
No.12	natMin	-1	--> arg1:even arg2:negative
No.13	natMax	intMin-1	--> Undefined Action
No.14	natMax	intMin	--> arg1:odd arg2:negative
No.15	natMax	intMax	--> arg1:odd arg2:positive
No.16	natMax	intMax+1	--> Undefined Action
No.17	natMax	0	--> arg1:odd arg2:positive
No.18	natMax	-1	--> arg1:odd arg2:negative
No.19	natMax+1	intMin-1	--> Undefined Action
No.20	natMax+1	intMin	--> Undefined Action
No.21	natMax+1	intMax	--> Undefined Action
No.22	natMax+1	intMax+1	--> Undefined Action
No.23	natMax+1	0	--> Undefined Action

No.24	natMax+1	-1	--> Undefined Action
No.25	2	intMin-1	--> Undefined Action
No.26	2	intMin	--> arg1:even arg2:negative
No.27	2	intMax	--> arg1:even arg2:positive
No.28	2	intMax+1	--> Undefined Action
No.29	2	0	--> arg1:even arg2:positive
No.30	2	-1	--> arg1:even arg2:negative
No.31	1	intMin-1	--> Undefined Action
No.32	1	intMin	--> arg1:odd arg2:negative
No.33	1	intMax	--> arg1:odd arg2:positive
No.34	1	intMax+1	--> Undefined Action
No.35	1	0	--> arg1:odd arg2:positive
No.36	1	-1	--> arg1:odd arg2:negative
No.37	3	intMin-1	--> Undefined Action
No.38	3	intMin	--> arg1:odd arg2:negative
No.39	3	intMax	--> arg1:odd arg2:positive
No.40	3	intMax+1	--> Undefined Action
No.41	3	0	--> arg1:odd arg2:positive
No.42	3	-1	--> arg1:odd arg2:negative

According to the specification,

- arg1:7, arg2:6 boundary values are output correctly
- Output the input data and the expected output data correctly as the boundary value test case

We input three specifications with different number of if-conditional expressions to BWDM, and measured the time until test cases are generated.

Times	specification1	specification2	specification3
1 st time	325	316	6277
2 nd time	283	389	5321
3 rd time	500	371	6236
4 th time	291	334	5070
5 th time	269	371	5700
Average	334	356	5720

We confirmed that boundary value test cases are automatically generated within a few seconds is the number of conditions is 15

Combinatorial Testing



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Overture* supports for Combinatorial Testing.

→ By conducting combinatorial test with test cases generated by BWDM, its possible to conduct more effective testing to find bugs.

*<http://overturetool.org/>

- In this research, we developed two tools to improve testing phase of software development with VDM++.
 - (1) VDTable : generates a decision table
 - (2) BWDM : generates boundary values
- We think that our tools have the potential of improving software testing process with VDM++.

Common issues of both tools

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- Evaluation by using huge specification that used in real development
- Correspondence to exponential explosion
- Expanding coverage of the tool
- Correspondence to other test design techniques

The issue of VTable

- Correspondence to compound conditional expression

The issue of BWDM

- Implementation of Symbolic Execution


```
#access
private
#location
in '/Users/katlab/Documents/workspace/VDMMDT/data/Sample.vdmpp' at line 4:3
#name
revBin2dec
#type
(seq of (nat) -> nat)
#kind
explicit function
#body
private revBin2dec: (seq of (nat) -> nat)
    revBin2dec(s) ==
(if (s = [])
then 0
elseif (s = [0])
then 0
elseif (s = [1])
then 1
else ((hd s) + (2 * revBin2dec((tl s))))))
```

#access

- types of access modifiers

#location

- location of VDM++ file
- start position of definition

#name

- name of definition

#type

- argument type

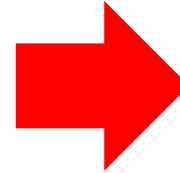
#kind

- types of definition

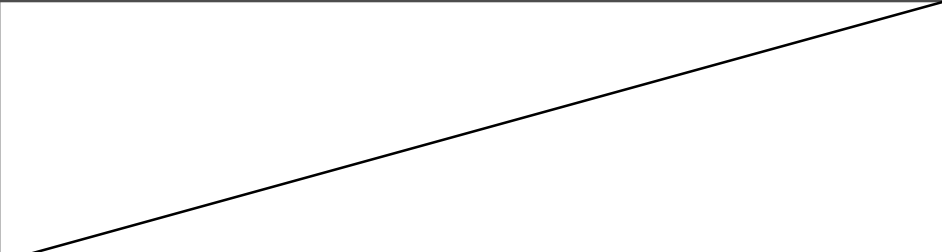
#body

- inside definition

```
...  
#kind  
explicit function  
#body  
private revBin2dec: (seq of (nat) -> nat)  
  revBin2dec(s) ==  
(if (s = [])  
  then 0  
  elseif (s = [0])  
  then 0  
  elseif (s = [1])  
  then 1  
  else ((hd s) + (2 * revBin2dec((tl s))))))
```



```
if1  
(s = [])  
then  
  0  
elseif  
(s = [0])  
then  
  0  
elseif  
(s = [1])  
then  
  1  
else1  
((hd s) + (2 * revBin2dec((tl s))))
```

condition extraction pattern	action extraction pattern
if “condition” then elseif “condition” then	then “action” if then “action” elseif then “action” else else “action” if else “action” elseif else “action” else else “action” EOF
cases “condition” ->	-> “action” cases others “Action” EOF
pre “condition” post pre “condition” EOF post “condition” EOF	

condition array

VTable : decision table

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internal representation data

condition array

```
if1
(s = [])
then
0
elseif
(s = [0])
then
0
elseif
(s = [1])
then
1
else1
((hd s) + (2 * revBin2dec((tl s))))
```

index	condition
0	(s = [])
1	(s = [0])
2	(s = [1])

extraction rule ※EOF(End Of File)

condition extraction pattern	action extraction pattern
if "condition" then elseif "condition" then	then "action" if then "action" elseif then "action" else else "action" else else "action" elseif else "action" else else "action" EOF
cases "condition" ->	-> "action" cases others "action" EOF
pre "condition" post pre "condition" EOF post "condition" EOF	

action array

VTable : decision table

internal representation data

action array

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```

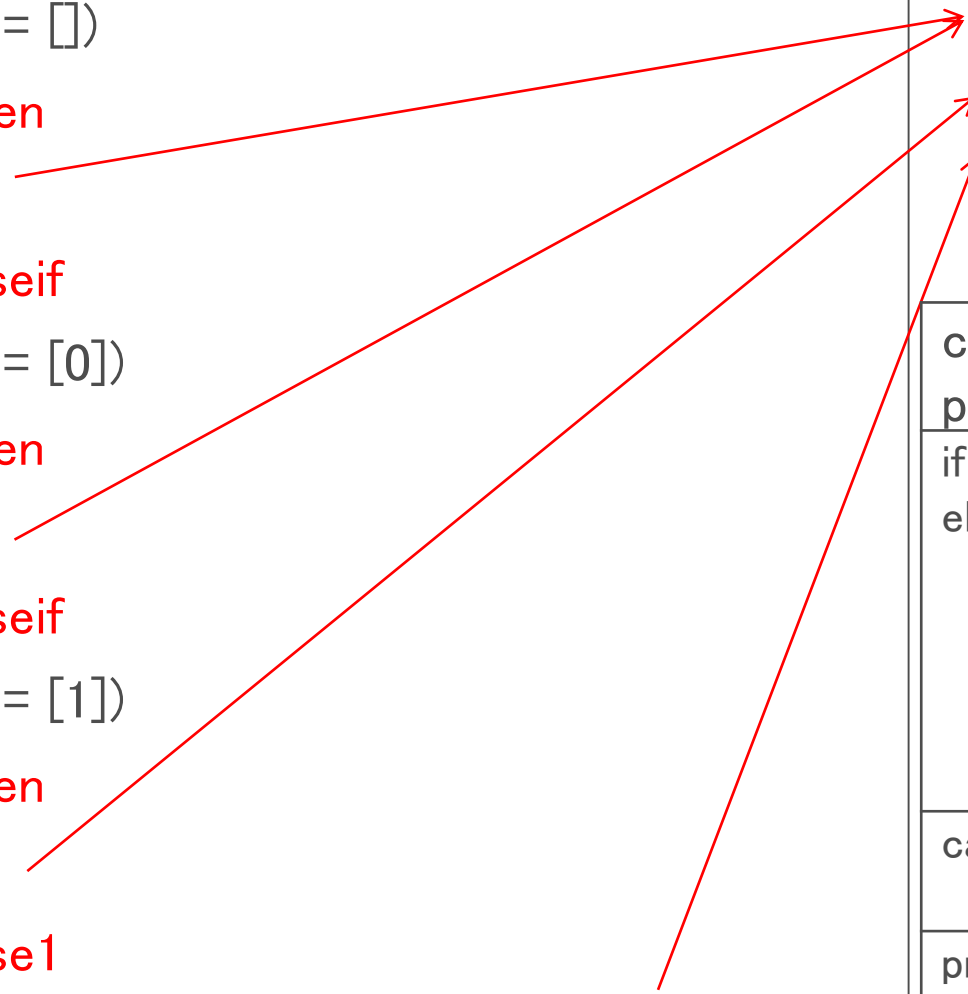
if1
(s = [])
then
0
elseif
(s = [0])
then
0
elseif
(s = [1])
then
1
else1
((hd s) + (2 * revBin2dec((tl s))))

```

index	action
0	0
1	1
2	((hd s) + (2 * revBin2dec((tl s))))

extraction rule ※EOF(End Of File)

condition extraction pattern	action extraction pattern
if "condition" then elseif "condition" then	then "action" if then "action" elseif then "action" else else "action" else else "action" elseif else "action" else else "action" EOF
cases "condition" ->	-> "action" cases others "action" EOF
pre "condition" post pre "condition" EOF post "condition" EOF	



condition-action table

VTable : decision table

internal representation data

```
if1  
(s = [])  
then  
0  
elseif  
(s = [0])  
then  
0  
elseif  
(s = [1])  
then  
1  
else1  
((hd s) + (2 * revBin2dec((tl s))))
```

index	condition
0	(s = [])
1	(s = [0])
2	(s = [1])

condition array 39

CA-Table

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

action array

index	action
0	0
1	1
2	((hd s) + (2 * revBin2dec((tl s))))

1. Create an array that is two dimensional and stores truth value.
2. Select the first column of the array.
3. Select a row of CA-Table from the first row.
4. Compare tokens and store truth value in the array
 - A) When “if”, “elseif”, “cases” are matched,
 - I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.
 - B) When “else”, “others” are matched,
 - I. Store "N" to the column selected for the conditional index row and "-" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.
5. If there are unselected rows, select the next column of the array and return to 3. When there is no, truth value is completed.

1. Create an array that is two dimensional and stores truth value.
2. Select the first column of the array.
3. Select one row of the CA-Table.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

condition index of	0	-	-	-	-
	1	-	-	-	-
	2	-	-	-	-
index of action	0	-	-	-	-
	1	-	-	-	-
	2	-	-	-	-

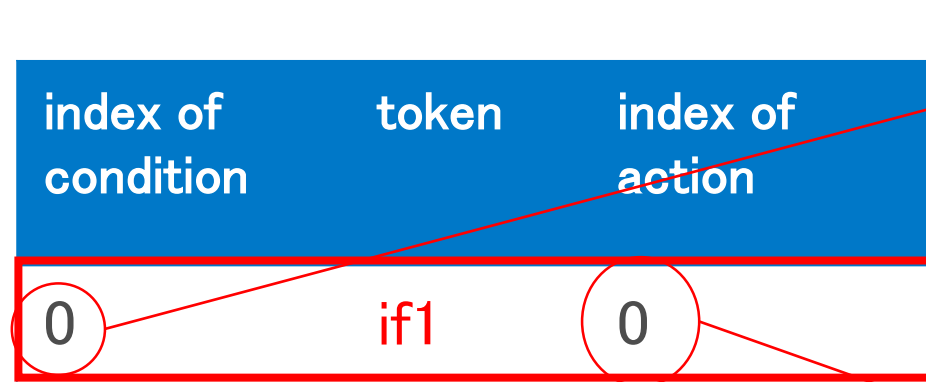
4. Compare tokens and store truth value in the array

- A) When “if”, “elseif”, “cases” are matched,
 - I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	-	-	-
2	-	-	-	-
0	X	-	-	-
1	-	-	-	-
2	-	-	-	-



condition

index of action

- If there are unselected rows, select the next column of the array and return to 3.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

condition	index of condition	0	Y	N	N	N
	1	-	-	-	-	
	2	-	-	-	-	
index of action	index of action	0	X	-	-	-
	1	-	-	-	-	
	2	-	-	-	-	

4. Compare tokens and store truth value in the array

- A) When “if”, “elseif”, “cases” are matched,
 - I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	Y	N	N
2	-	-	-	-
0	X	X	-	-
1	-	-	-	-
2	-	-	-	-

index of condition

index of action

4. Compare tokens and store truth value in the array

- A) When “if”, “elseif”, “cases” are matched,
 - I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

index of condition	0	1	2	3
0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N

index of action	0	1	2	3
0	X	X	-	-
1	-	-	X	-
2	-	-	-	-

4. Compare tokens and store truth value in the array

B) When "else", "others" are matched,

- I. Store "N" to the column selected for the conditional index row and "-" from the next column to the end of the column.
- II. Store "X" in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N
0	X	X	-	-
1	-	-	X	-
2	-	-	-	X

- If there are unselected rows, select the next column of the array and return to 3.

When there is no, truth value is completed.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

condition index of	0	Y	N	N	N
	1	-	Y	N	N
	2	-	-	Y	N

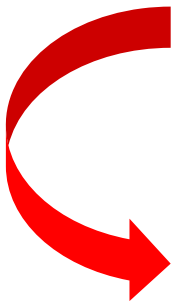
index of action	0	X	X	-	-
	1	-	-	X	-
	2	-	-	-	X

index	condition
0	(s = [])
1	(s = [0])
2	(s = [1])

index	action
0	0
1	1
2	((hd s) + (2 * revBin2dec((tl s))))

0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N

0	X	X	-	-
1	-	-	X	-
2	-	-	-	X



Rule	#1	#2	#3	#4
Condition				
(s = [])	Y	N	N	N
(s = [0])	-	Y	N	N
(s = [1])	-	-	Y	N
Action				
0	X	X	-	-
1	-	-	X	-
((hd s) + (2 * revBin2dec((tl s))))	-	-	-	X

CEGTest*

The tool for automatically generating a decision table.

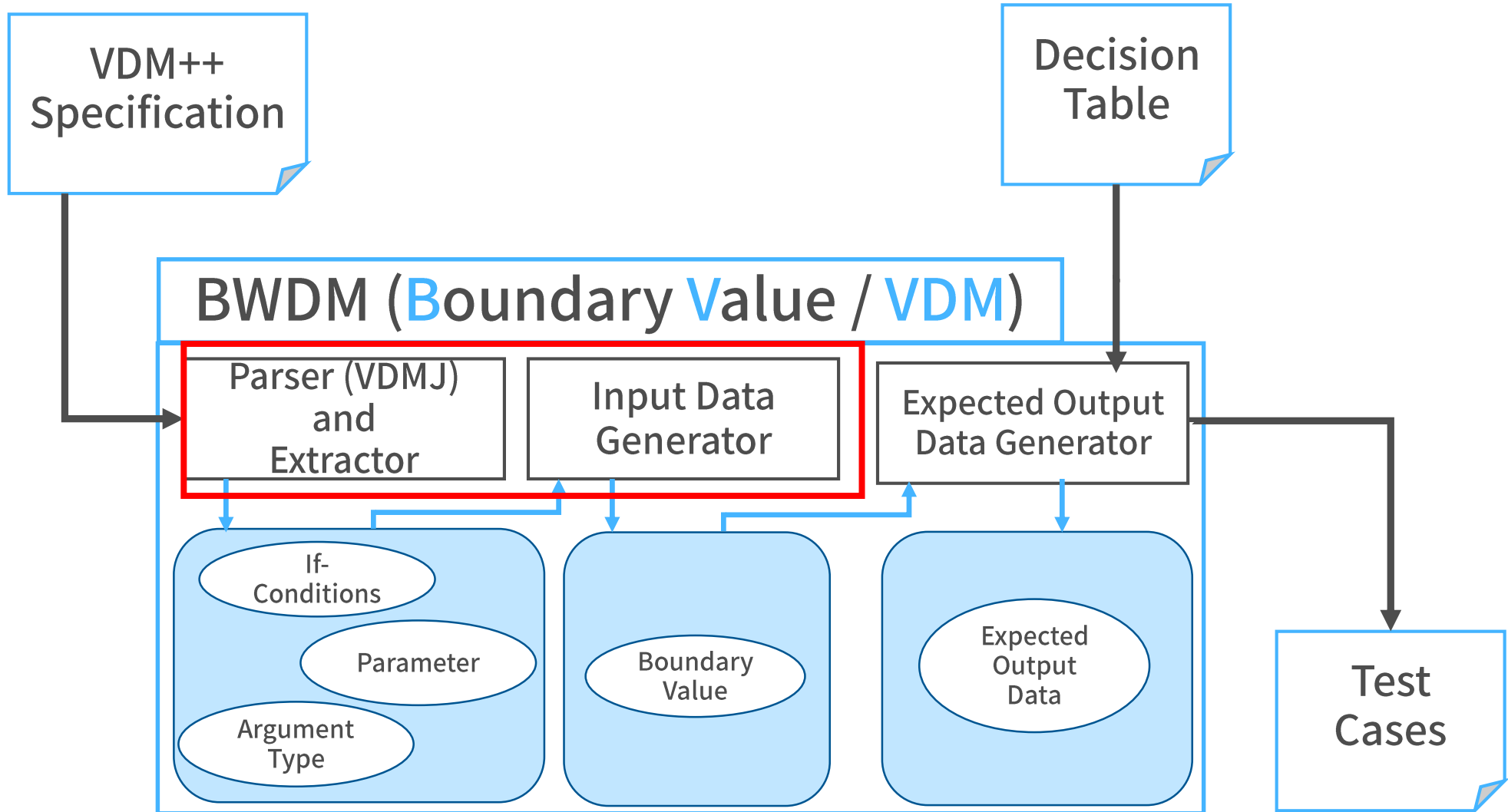
The cause result graph as the input of CEGTest has to be created manually by the user from the VDM++ specification.

→ VDTable only needs a VDM++ specification for input.

*<http://softest.jp/tools/CEGTest/>

- Function definition is only supported definition of VDM++ .
- The number of arguments is limited to one or two.
- The type of arguments is limited to Integer. (int, nat, nat1)
- If-conditions are limited to inequalities and modulo.
- If-conditions are limited to those not connected by “and”, “or”.
- If-conditions are limited to ones whose sides are not variables.

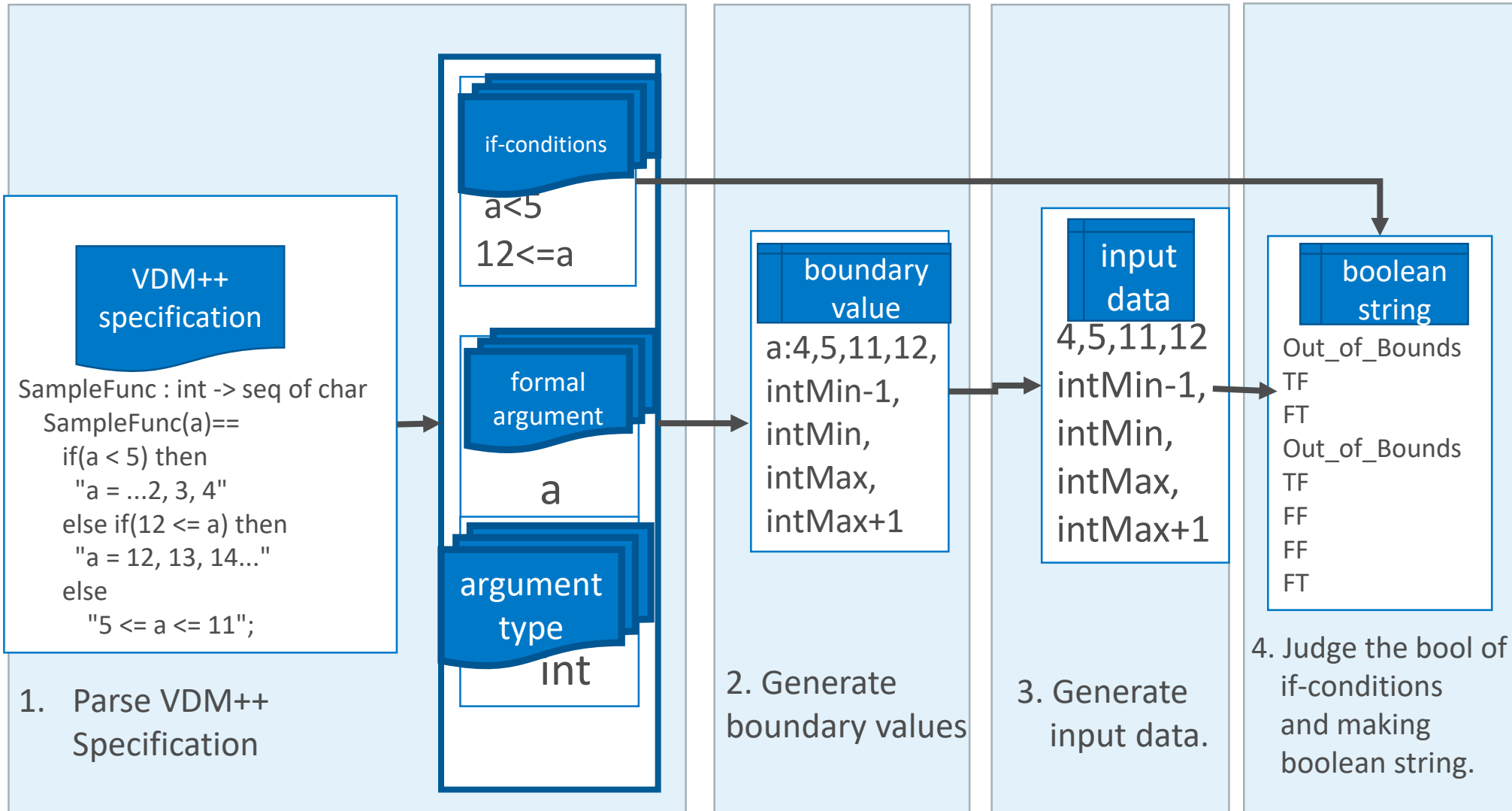
Explain process of making input data.



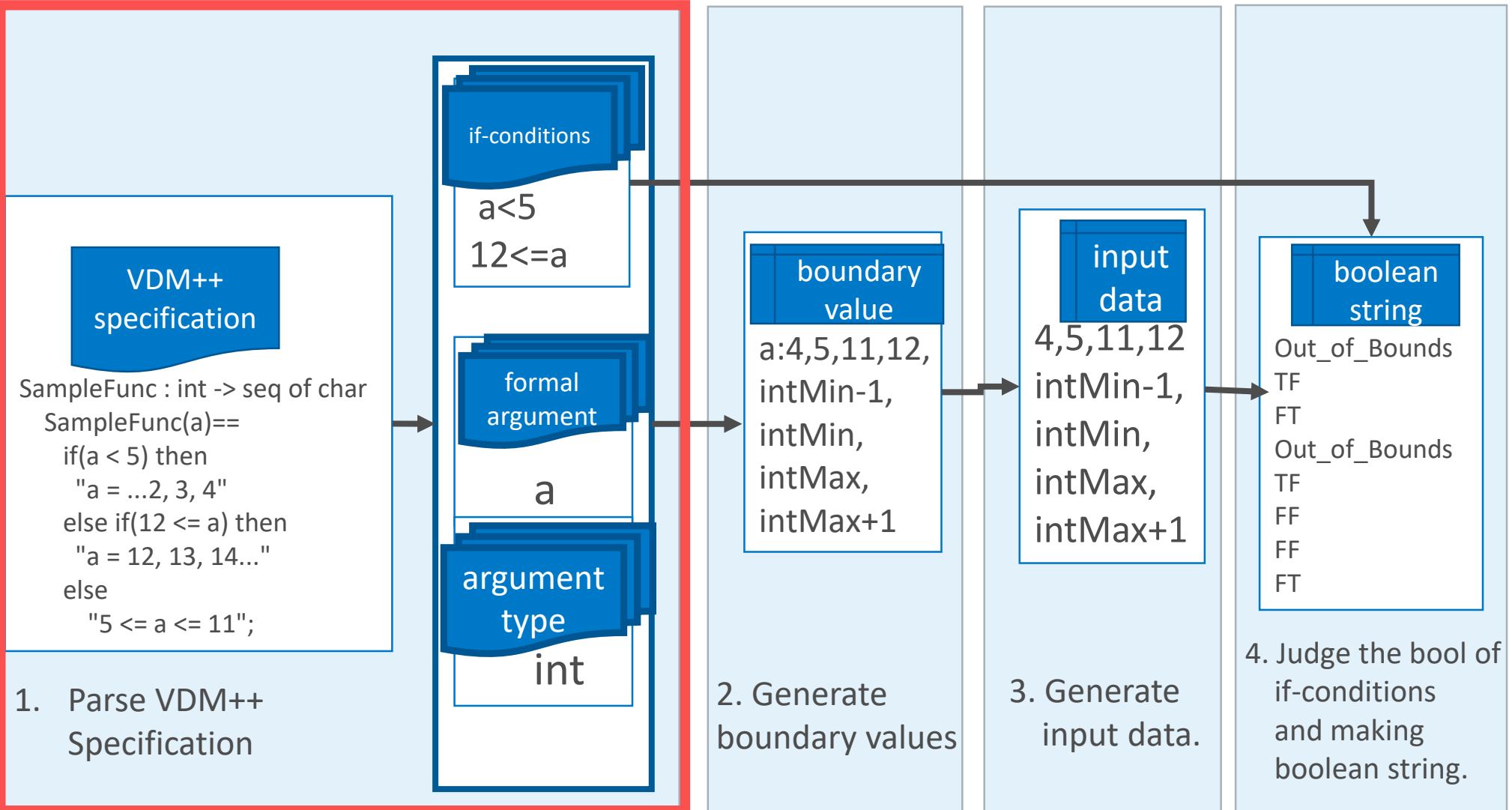
Following four processes are performed for making input data

1. Parse VDM++ specification
2. Generate boundary values
3. Generate input data
4. Generate boolean strings

Overview of the process flow



1. Parse VDM++ specification

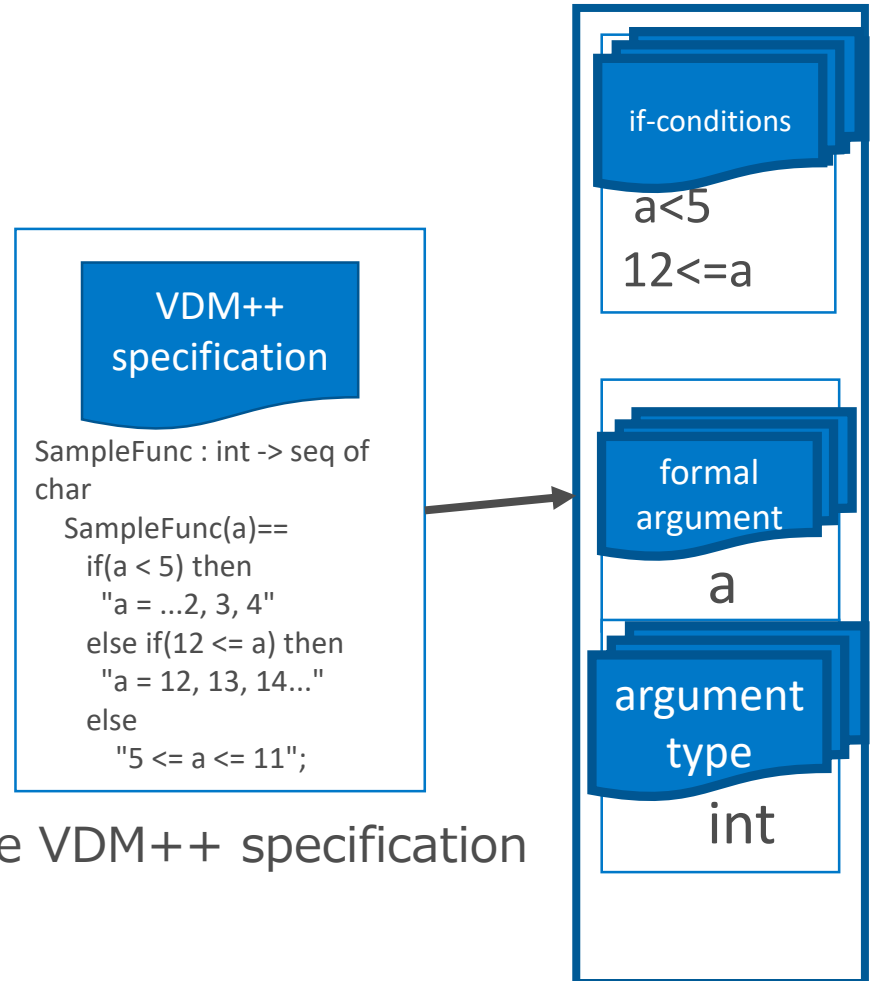


1. Parse VDM++ specification

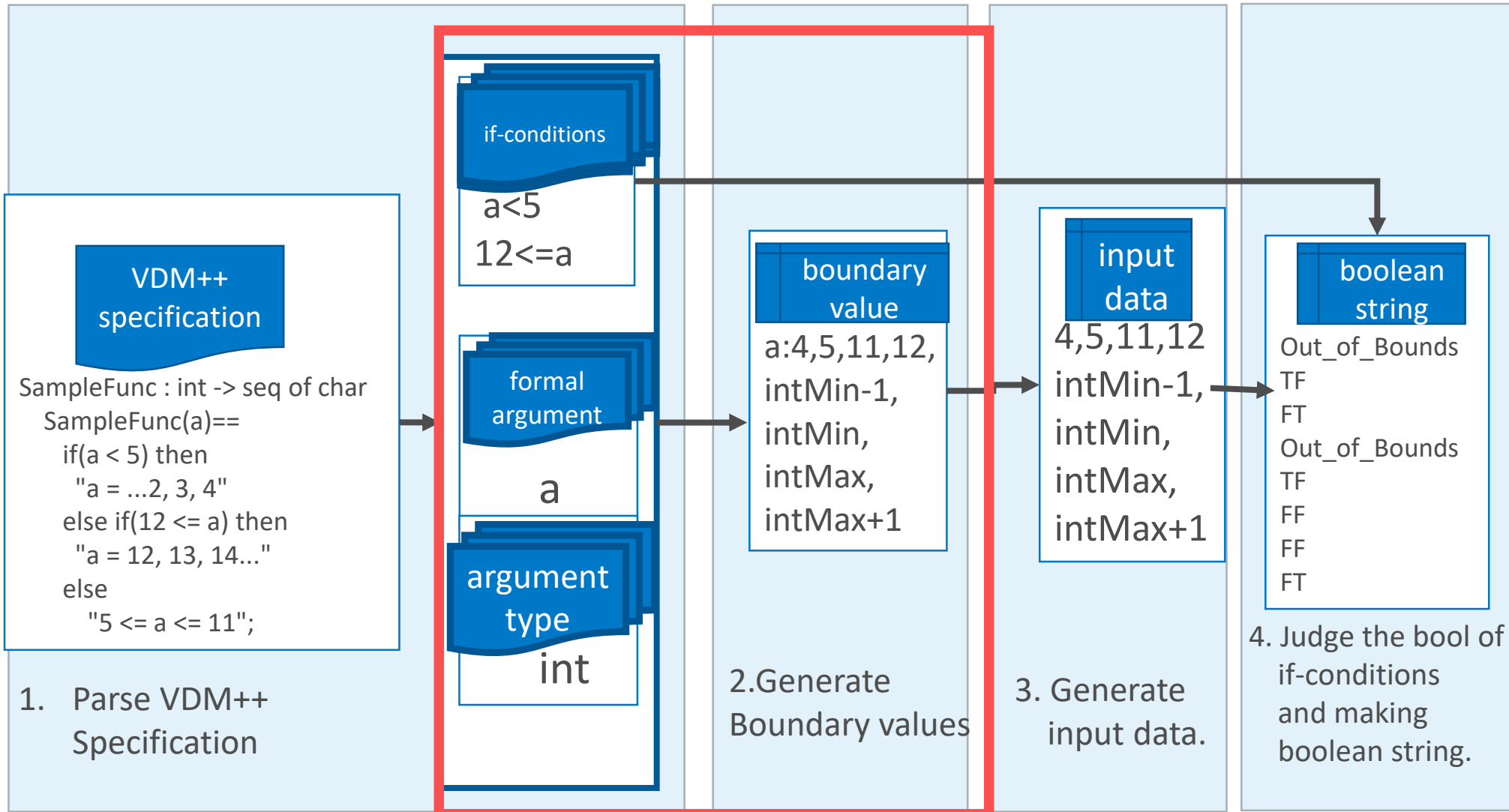
Parse VDM++ specification
by using VDMJ



Extract argument types,
formal arguments, and
if-conditions



2. Generate boundary Values



2. Generate boundary Values

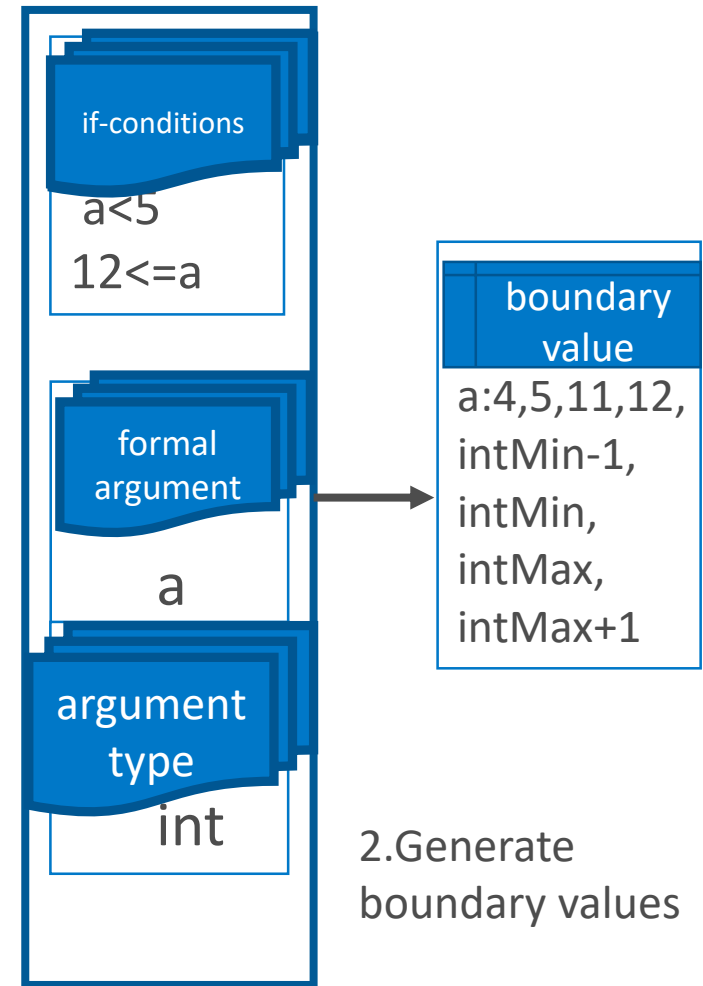
Based on the extracted information, generate boundary values.

type boundary value

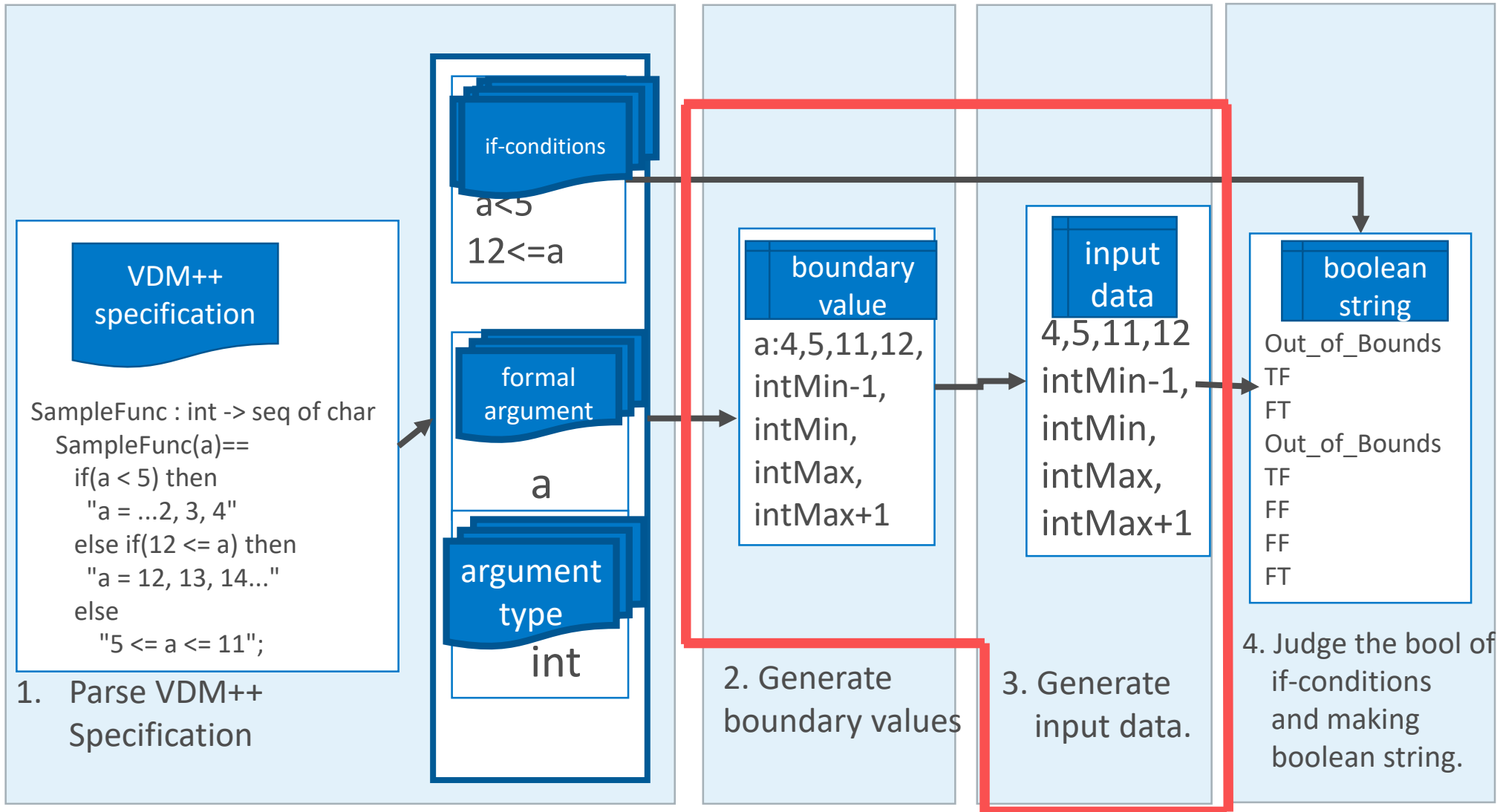
- Generate minimum value, maximum value, minimum value-1, maximum value+1 of argument type

if-condition boundary value

- Generate two boundary values in case of inequality
- three values in case of modulo;
a value that satisfies “=” and two values of ± 1 of it



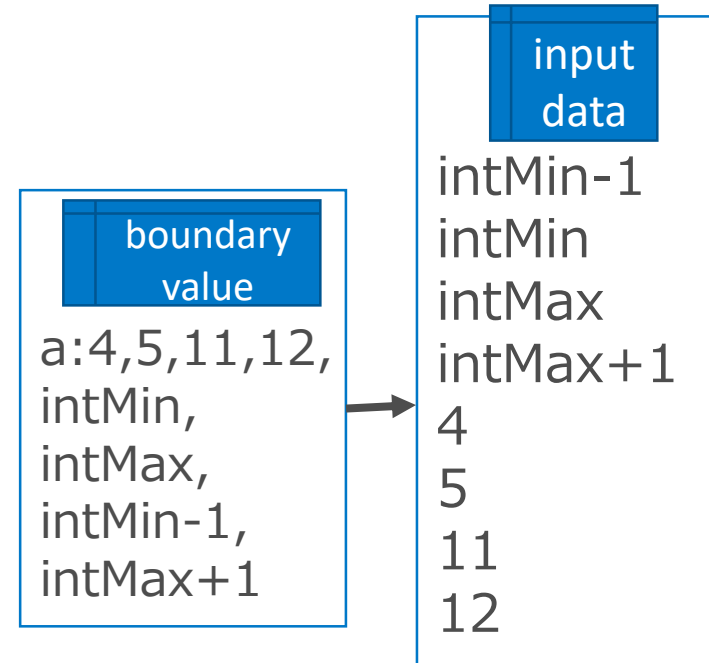
• 3. Generate Input Data



3. Generate Input Data

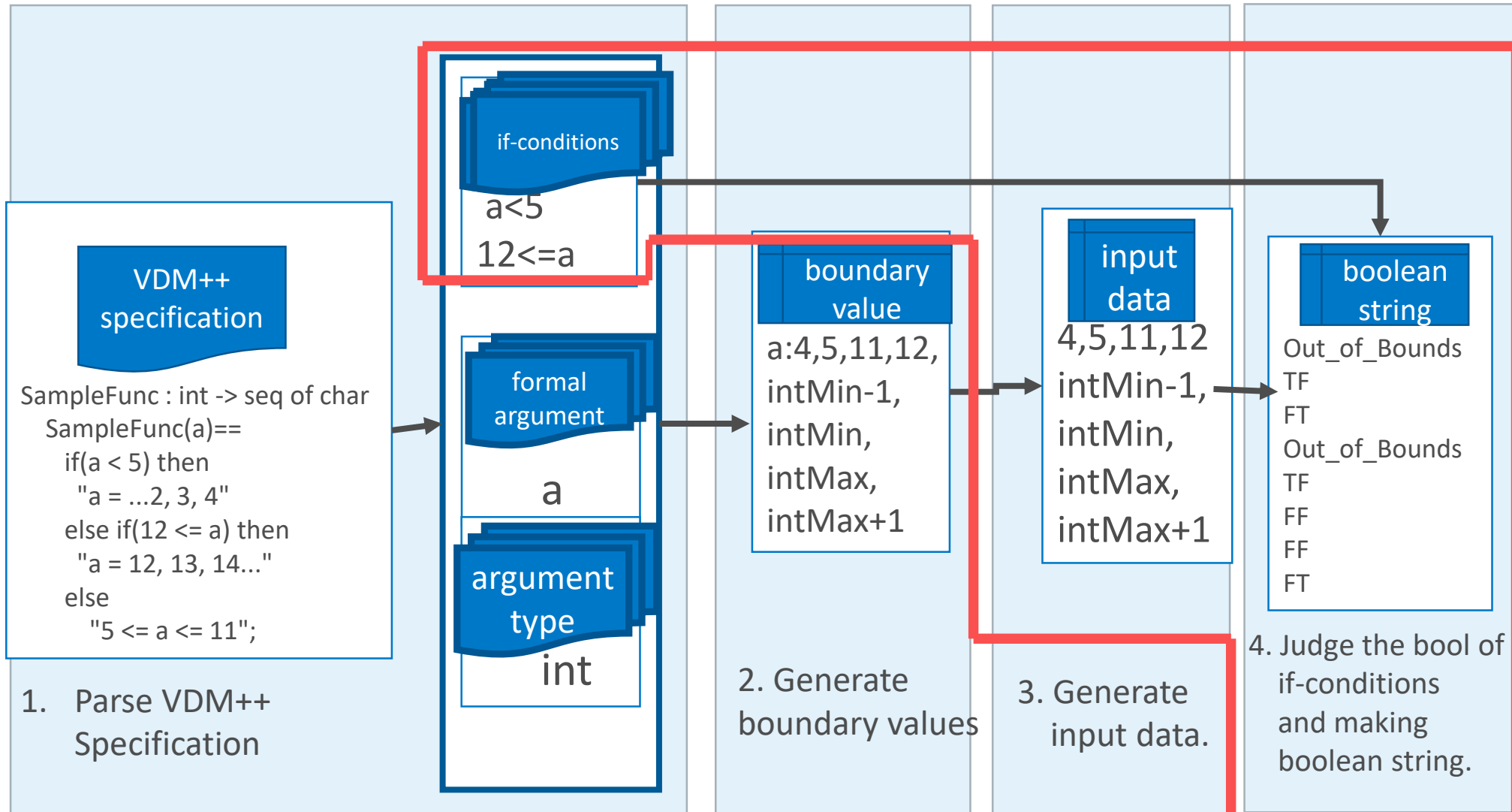
Generate input data from generated boundary value

In the case of two arguments, all combinations of boundary values of each arguments are generated for input data.



3. Generate input data

• 4. Generate Boolean Strings



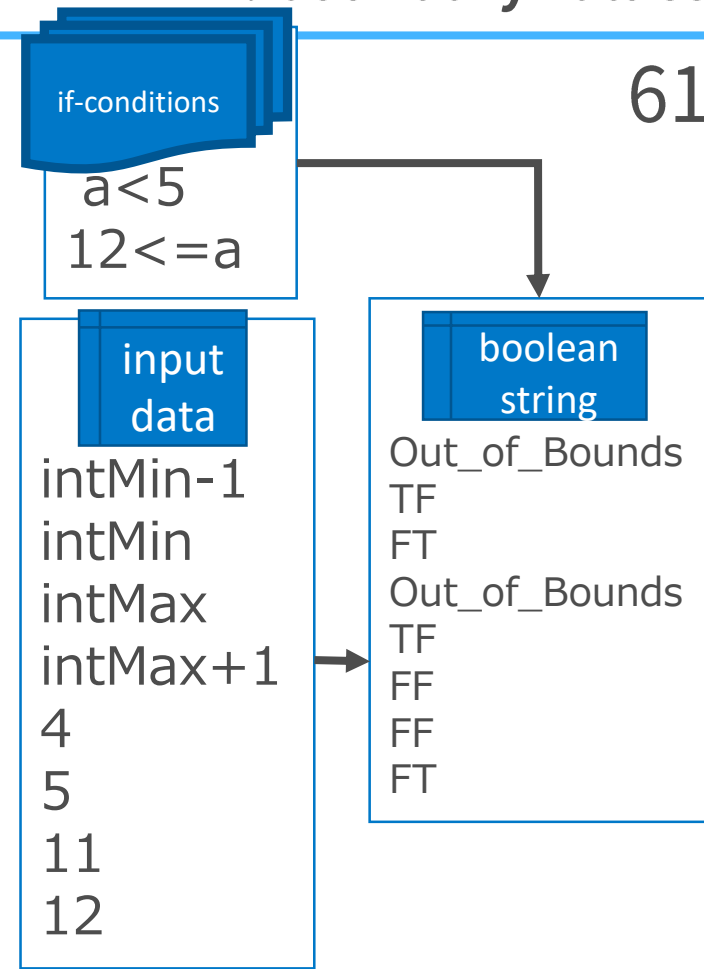
making input data

4. Generate Boolean Strings

Generate Boolean strings from the generated input data and if-conditional expressions

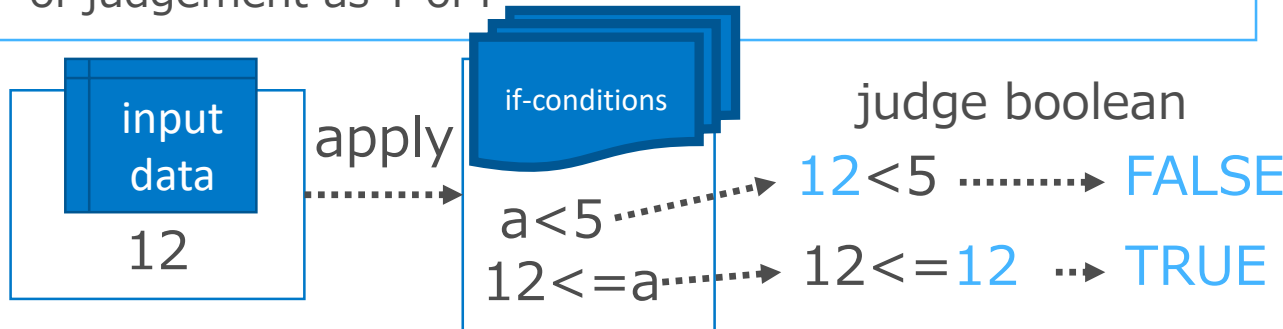


used in the expected output data generator



Boolean String

- Assigning input data to the if-conditional expressions to determine a Boolean value and characterizing the result of judgement as T of F

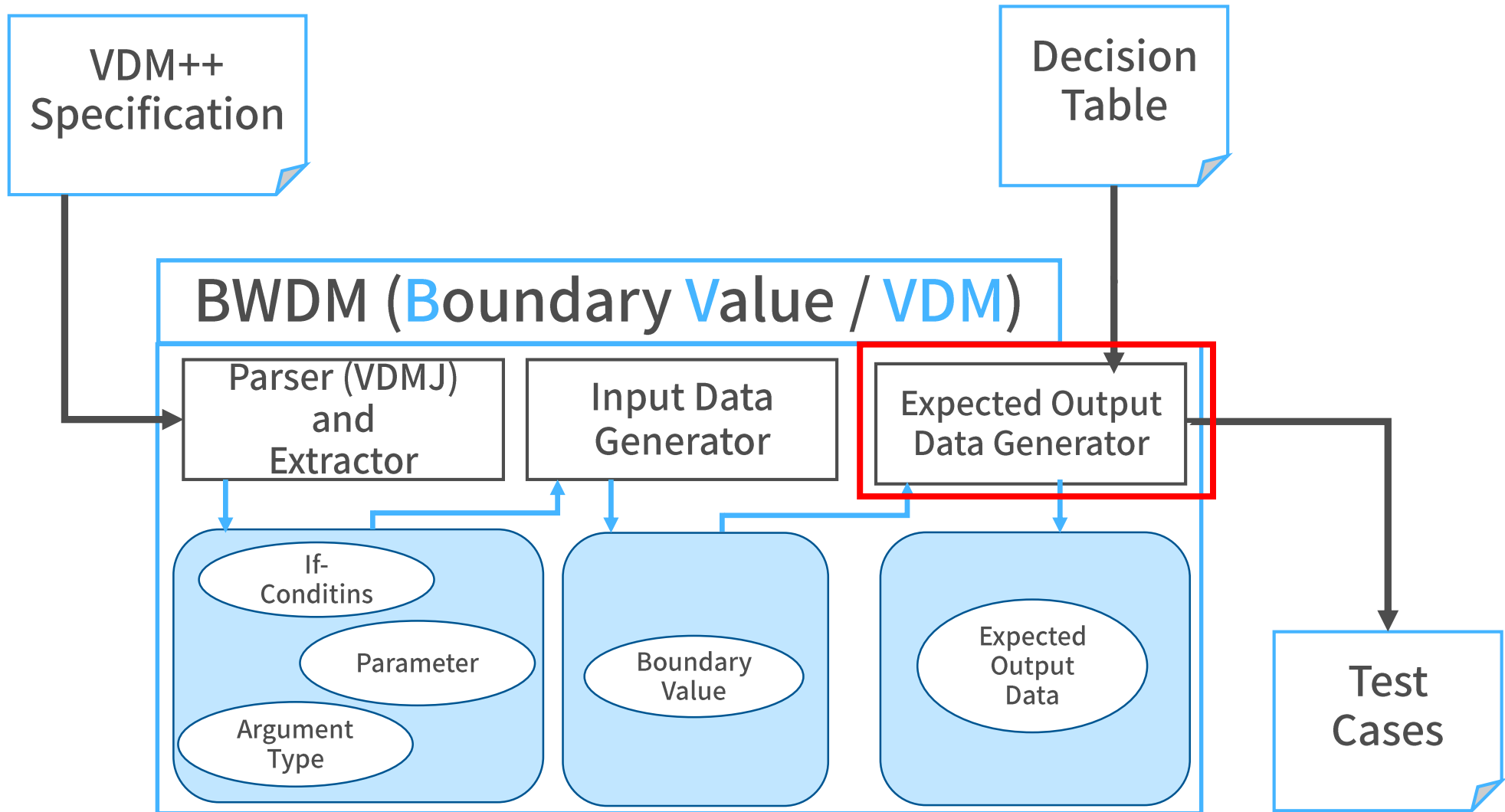


4. Judge the bool of if-conditions and making boolean string.

"FT"

figure: Example of creating a Boolean string "FT" from input data "1, 2" and if-conditional expressions "a < 5, 12 <= a"

Explain process of making expected output data.



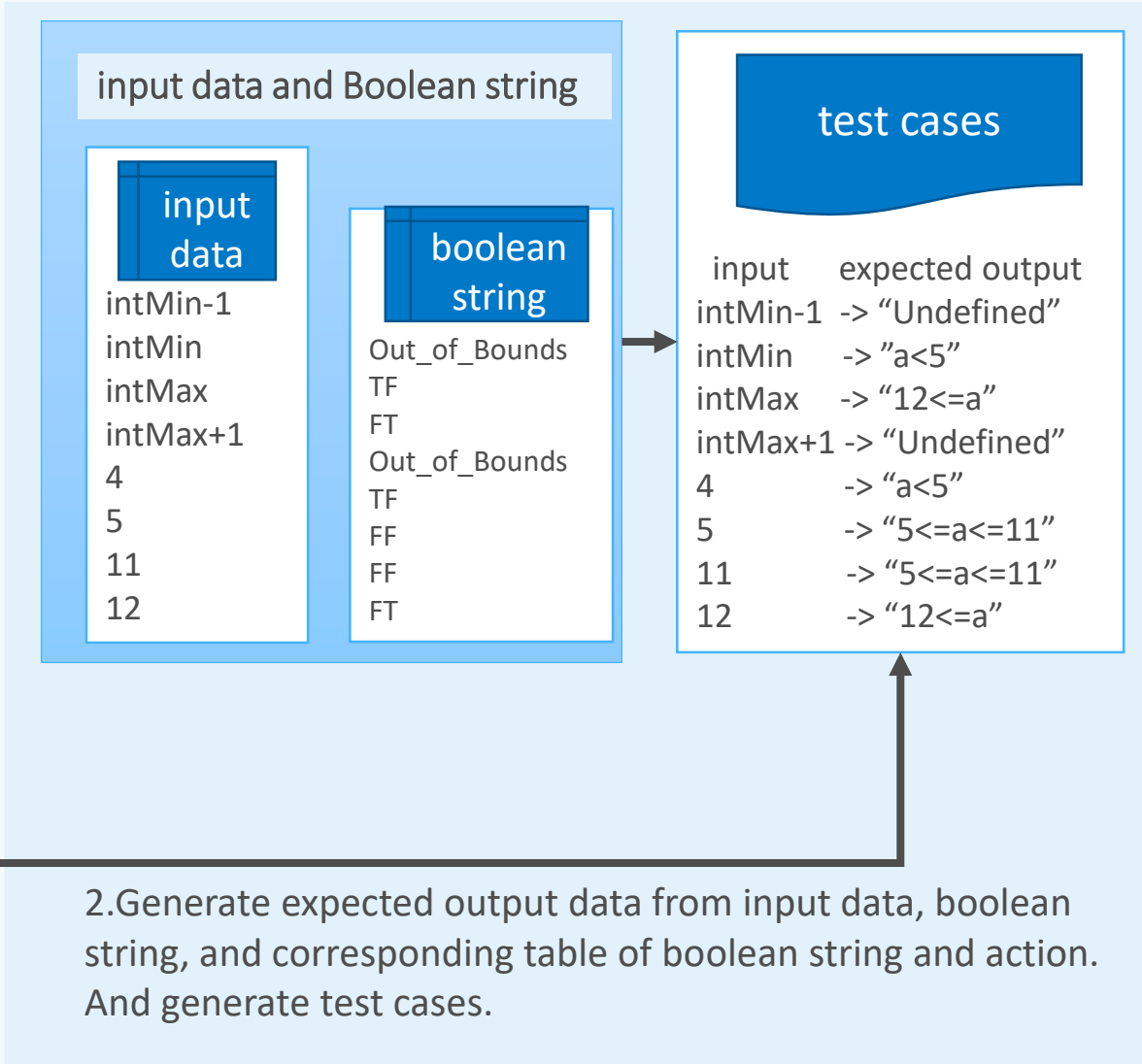
Following two steps are performed to make expected output data.

1. Load decision table and generate corresponding table of Boolean string and action
2. Generate expected output data and test cases

• Overview of the Process Flow

Decision Table		#1	#2	#3	#4
Condition	$a < 5$	T	T	F	F
Condition	$12 \leq a$	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5<=a<=11"	F	F	F	T

corresponding table of boolean strings and actions	
boolean string	action
TT	"a<5"
TF	"a<5"
FT	"12<=a"
FF	"5<=a<=11"



2. Generate expected output data from input data, boolean string, and corresponding table of boolean string and action. And generate test cases.

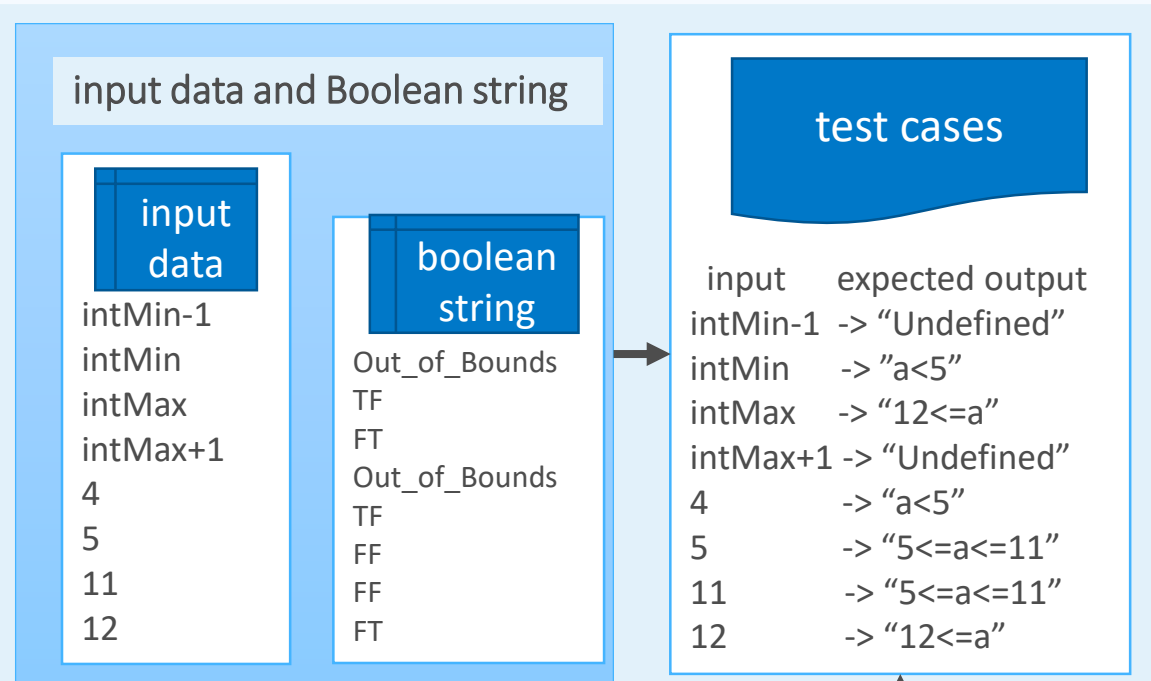
1. Load decision table and generating table of Boolean string and action.

making expected output data

- 1. Load decision table and generate table of Boolean strings and actions

Decision Table					
		#1	#2	#3	#4
Condition	a < 5	T	T	F	F
Condition	12 <= a	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5<=a<=11"	F	F	F	T

corresponding table of boolean strings and actions	
boolean string	action
TT	"a<5"
TF	"a<5"
FT	"12<=a"
FF	"5<=a<=11"



input	expected output
intMin-1	-> "Undefined"
intMin	-> "a<5"
intMax	-> "12<=a"
intMax+1	-> "Undefined"
4	-> "a<5"
5	-> "5<=a<=11"
11	-> "5<=a<=11"
12	-> "12<=a"

2. Generate expected output data from input data, boolean string, and corresponding table of boolean string and action. And generate test cases.

1. Load decision table and generating table of Boolean string and action.

- 1. Load decision table and generate table of Boolean strings and actions

Load the decision table that generated by VDTTable.



Generate correspondence table of Boolean strings and actions.

Decision Table					
		#1	#2	#3	#4
Condition	$a < 5$	T	T	F	F
Condition	$12 \leq a$	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 ≤ a"	F	F	T	F
Action	"5 ≤ a ≤ 11"	F	F	F	T

corresponding table of boolean strings and actions	
boolean string	action
TT	"a<5"
TF	"a<5"
FT	"12≤a"
FF	"5≤a≤11"

1. Load decision table and generating table of Boolean string and action.

2. Generate expected output data and test cases

Decision Table		#1	#2	#3	#4
Condition	$a < 5$	T	T	F	F
Condition	$12 \leq a$	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5<=a<=11"	F	F	F	T

corresponding table of Boolean string and action	
boolean string	action
TT	"a<5"
TF	"a<5"
FT	"12<=a"
FF	"5<=a<=11"

input data and Boolean string

<p style="text-align: center; background-color: #0056b3; color: white; padding: 5px;">input data</p> <p>intMin-1 intMin intMax intMax+1 4 5 11 12</p>	<p style="text-align: center; background-color: #0056b3; color: white; padding: 5px;">boolean string</p> <p>Out_of_Bounds TF FT Out_of_Bounds TF FF FF FT</p>
---	---

test cases

input	expected output
intMin-1	-> "Undefined"
intMin	-> "a<5"
intMax	-> "12<=a"
intMax+1	-> "Undefined"
4	-> "a<5"
5	-> "5<=a<=11"
11	-> "5<=a<=11"
12	-> "12<=a"

2. Generate expected output data from input data, boolean string, and corresponding table of boolean string and action. And generate test cases.

1. Load decision table and generating table of Boolean string and action.

2. Generate Expected Output Data and Test Cases

Generate expected output data from input data, boolean strings, and corresponding table of boolean string and action.



Finally, BWDM outputs test cases that consist input data and expected output data.

